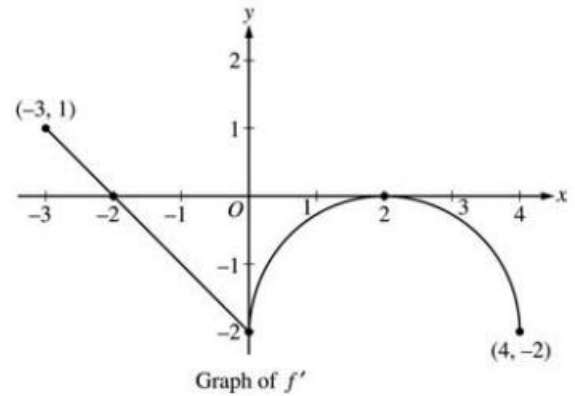


Station1: Accumulation Graph

Let f be a function defined on the closed interval $[-3,4]$ with $f(0) = 3$. The graph of f' , the derivative of f , consists of one-line segment and a semicircle, as shown.

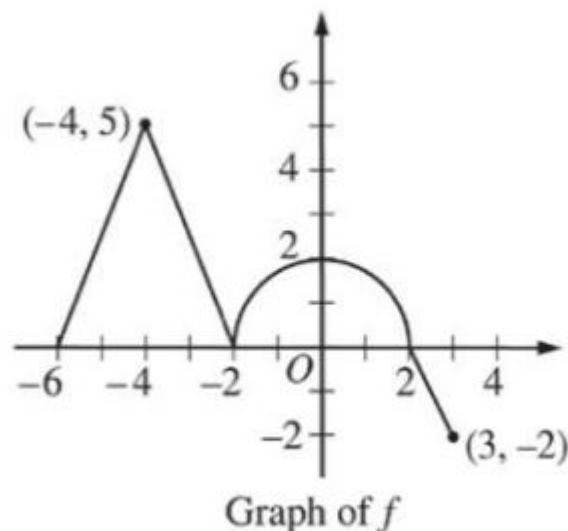


1. On what intervals, if any is f increasing? Justify.
2. Find $f(-3)$.
3. Find the equation of the tangent line to the function f at the point $(0, -3)$

The graph of the continuous function f , consisting of three line segments and a semicircle is shown below. Let g be the function given by

$$g(x) = \int_{-2}^x f(t) dt$$

4. Find $g(-6)$ and $g(0)$.
5. Find all the values of x on the open interval $(-6, 3)$ for which the graph of g has a horizontal tangent. Determine whether g has a local max, local min, or neither at each of these values. Justify.



Station 2: Integration

1. $\int (x - 2)\sqrt{x + 3} dx$

2. $\int \frac{5dx}{x \ln x}$

3. $\int \left(x^{\frac{1}{3}} + x\sqrt{x} - 2 \right) dx$

4. $\int (e^{-x} + \sec^2(\frac{x}{3})) dx$

Station 3: More Integration

1. $\int_2^{-4} |2 + x| dx$

2. $\int_0^{1/2} [e^y + 2 \cos(\pi y)] dy =$

3. Find the particular solution that satisfies the differential equations and the initial conditions.

$$f''(x) = \frac{2}{x^2}, f'(1) = 1, f(1) = 1, x > 0$$

4. $\int_0^3 \frac{2e^{2x}}{1+e^{2x}} dx$

Station 4: Average Value and FTC (2)

1. $\frac{d}{dx} \left(\int_{\cos(x^2)}^{2x} x^2 dx \right) =$

2. Given $F(x) = \int_0^{e^{2x}} \ln(t + 1) dt$, find $F'(x)$.

3. The acceleration at time t of an object is given by $a(t) = 4\pi \cos t$. What is the average acceleration of the object over the interval $[0, \pi]$?

4. Find the number(s) c guaranteed by the Mean Value Theorem for Integrals for $\int_0^{2\pi} \cos x dx$.

Station 5: Approximation

The diameter of a tunnel $h(x)$ measured in feet is given in different intervals on the table below, with $h'(x) > 0$.

x	5	8	11	13	15	17	19
$h(x)$	5	6	8	10	11	13	16

1. Use trapezoids to estimate $\int_5^{19} h(x) dx$.

2. Use MRAM to estimate $\int_5^{19} h(x) dx$.

3. Find the average diameter of the tunnel using your answers from question #1. Include unit of measure.

4. If you use RRAM, would it be more than or less than the value of $\int_5^{19} h(x) dx$. Justify your answer.