

Volumes of Revolution Homework  
AP Calculus

Name: \_\_\_\_\_

Draw all defined regions without the use of a calculator. Then use the calculator to find intersections and evaluate the problem.

(1) Region  $R$  is bounded by  $y = x^2 - 3$ ,  $x = 6$ , and the  $x$ -axis. Find the volume when  $R$  is rotated around the line:

- (A)  $y = 6$                       (B)  $y = -2$                       (C)  $x = 6$                       (D)  $x = 1$

(2) Region  $S$  is bounded by the functions  $y = \sqrt{x}$ ,  $y = -\ln x$ , and  $x = 3$ . Find the volume when  $S$  is rotated around the line:

- (A)  $y = 3$                       (B)  $y = -4$                       (C)  $x = 3$  (be careful)

(3) Region  $T$  is bounded by the graphs of  $y = x^2$ ,  $y = 0$ , and  $x = 4$ .

(A) Find the value of  $a$  such that the line  $x = a$  divides  $T$  into two equal areas.

(B) If  $T$  is rotated about the  $x$ -axis, find the value of  $b$  such that the line  $x = b$  divides the solid into two equal volumes.

(C) If  $T$  is rotated about the line  $x = -1$ , find the value of  $c$  such that the line  $y = c$  divides that solid into two equal volumes.