

Polar Review  
AP Calculus

Name: \_\_\_\_\_

Find the slope of the tangent line to the graphs at the indicated points.

- (a)  $r = \cos\theta$  at  $\theta = 0, \pi/4$
- (b)  $r = \sin(5\theta)$  at  $\theta = 0, \pi/2$

Find the points where the indicated graphs have horizontal and vertical tangent lines.

- (a)  $r = \cos\theta$
- (b)  $r = \sin(4\theta)$
- (c)  $r = 5\cos\theta$

Find the area of the following curves.

- (a) interior of  $r = \sin\theta$
- (b)  $r = \sin 5\theta$  (all petals)
- (c)  $r = \sin 5\theta$  (the petal in the 3<sup>rd</sup> quadrant with proper limits)
- (d)  $r = 3 - 5\sin\theta$  (area of the outer loop)

Find the area bounded by the following sets of equations.

- (a) Bounded inside of  $r = 6\sin 2\theta$  and outside of  $r = 3$  in Quadrant 1.
- (b) Common area of  $r = 6\sin 2\theta$  and  $r = 3$  on the whole  $xy$ -plane.
- (c) Inside  $r = 3\cos\theta$  and outside  $r = 2 - \cos\theta$ .
- (d) Common interior of  $r = 3\cos\theta$  and  $r = 1 + \cos\theta$ .
- (e) Inside  $r = 3\sin\theta$  and outside  $r = 1 + \sin\theta$ .

Multiple Choice

The area enclosed inside the polar curve  $r^2 = 10\cos 2\theta$  is

- (A) 10
- (B)  $5\pi$
- (C) 20
- (D)  $10\pi$
- (E)  $25\pi$

The area enclosed by the polar curve  $r \cos \frac{1}{2}\theta = 1$  in the interval  $0 \leq \theta \leq \frac{\pi}{2}$  is

- (A)  $\frac{1}{2}$
- (B)  $\frac{\sqrt{2}}{2}$
- (C)  $\frac{\pi}{4}$
- (D) 1
- (E) 2

Free Response

The graphs of the polar curves  $r = 2$  and  $r = 3 + 2\cos\theta$  can be graphed in the  $xy$ -plane.

- (a) Let  $R$  be the region that is inside the graph of  $r = 2$  and also inside the graph of  $r = 3 + 2\cos\theta$ . Find the area of  $R$ .
- (b) A particle moving with nonzero velocity along the polar curve given by  $r = 3 + 2\cos\theta$  has a position  $(x(t), y(t))$  at time  $t$ , with  $\theta = 0$  when  $t = 0$ . This particle moves along the curve so that  $\frac{dr}{dt} = \frac{dr}{d\theta}$ . Find the value of  $\frac{dr}{dt}$  at  $\theta = \frac{\pi}{3}$  and interpret your answer in terms of the motion of the particle.
- (c) For the particle described in part (b),  $\frac{dy}{dt} = \frac{dy}{d\theta}$ . Find the value of  $\frac{dy}{dt}$  at  $\theta = \frac{\pi}{3}$  and interpret your answer in terms of the motion of the particle.